

Algorithmic Combinatorics  
Exercises discussed on May 27, 2019

43. Compute a hypergeometric closed form of the sum  $s_n = \sum_{k=0}^n \frac{4}{(2k-1)(2k+1)}$  by applying Gosper's algorithm.
44. Show that the harmonic numbers are not hypergeometric using Gosper's algorithm.
45. For which values of  $\alpha$  is  $a_k = \binom{2k}{k} \alpha^k$  Gosper summable? Compute  $\sum_{k=0}^n a_k$  for the admissible values of  $\alpha$ .