

# Model Checking

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# Outline

- Overview
- Kripke Structures
- Temporal Logics (CTL\*, CTL, LTL)
- Model Checking Problem
- Büchi Automata
- Solution algorithm
- State explosion problem
- Model-checking in practice

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- Uses temporal logic to reason about the correctness of a system
- Works with finite-state concurrent system.

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  - Testing cannot cover all the possible cases.

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  - If the result is **no**, counter-example needs to be analyzed to discover the source of the bug.

# Kripke Structure

A formalism for specifying the possible states of a system and their transition relations.

## Definition

A *Kripke Structure*  $M$  over a set of atomic propositions  $AP$  is a 4-tuple:

$$M = \langle S, S_0, R, L \rangle$$

where:

- 1  $S$  is a finite set of states.
- 2  $S_0 \subseteq S$  is the set of starting states.
- 3  $R \subseteq S \times S$  is a transition relation.
- 4  $L : S \rightarrow \mathcal{P}(AP)$  is function that labels each state with the set of propositions that are true in that state.

Alternative definition for  $L : S \rightarrow (AP \rightarrow \{\top, \perp\})$

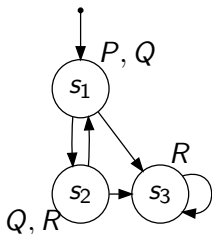
# Kripke Structure Example

Define Kripke Structure  $M_1$  over the atomic propositions  $AP = \{P, Q, R\}$  as follows:

$$M_1 = \langle \{s_1, s_2, s_3\}, \{s_1\}, R_1, L_1 \rangle$$

where:

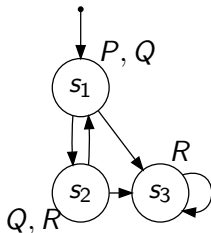
- $R_1 = \{(s_1, s_2), (s_2, s_1), (s_1, s_3), (s_2, s_3), (s_3, s_3)\}$
- $L_1 = \{(s_1 \rightarrow \{P, Q\}), (s_2 \rightarrow \{Q, R\}), (s_3 \rightarrow \{R\})\}$



## Definition (Path)

A *path*  $\pi$  in a Kripke Structure  $M = \langle S, S_0, R, L \rangle$  is an infinite sequence of states  $s_0, s_1, \dots$  such that for each  $i \geq 0$ ,  $(s_i, s_{i+1}) \in R$ .

- The notation  $\pi^i$  refers to the subsequence of  $\pi$  starting at  $s_i$  (i.e.  $s_i, s_{i+1}, \dots$ )
- Kripke Structure unwinding



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- In model-checking, temporal modal logics are used to specify the desirable properties of the system.
- Commonly used TLs are CTL\*, CTL, and LTL.
- LTL is a *linear-time logic*
- CTL and CTL\* are *branching-time logics*

- stands for "Computational Tree Logic\*"
- is a superset of LTL and CTL.
- CTL\* has 2 types of formulas:
  - 1 Path formulas: specify properties of a given path.
  - 2 State formulas: specify properties of a given state.

## CTL\* Path Operators

- **X**  $f$  ("Next"): The property  $f$  holds in the *next state* of the given path.
- **F**  $f$  ("future"): The property  $f$  holds *finally* (eventually).
- **G**  $f$  ("globally"): The property  $f$  holds *globally* (in all future states of the path).
- $f$ **U**  $g$  ("until"): Property  $f$  must hold *until*  $g$  holds.  $g$  is required to become true eventually.
- $f$ **R**  $g$  ("release"): Property  $g$  must hold up-to and including the first state in which  $f$  holds.  $g$  is *released* by  $f$ .
- **Examples:**  $P$ **U**  $Q$ ,  $P$ **R**  $Q$ .



- Given a set of atomic propositions  $AP$ ,
- the syntax of **state formulas** is defined as follows:
  - ① every proposition  $p \in AP$  is a state formula. (Holds if  $p$  is true in the given state)
  - ② If  $f$  and  $g$  are state formulas, then  $\neg f$ ,  $f \wedge g$ ,  $f \vee g$  are state formulas.
  - ③ If  $f$  is a *path formula*, the  $Af$  and  $Ef$  are state formulas.
- **A** and **E** are path quantifiers.
- The syntax of **path formulas** is defined as follows:
  - ① If  $f$  is a *state formula* then  $f$  is also a path formula. (Holds if  $f$  is true in the first state of the path)
  - ② If  $f$  and  $g$  are *path formulas* then  $\neg f$ ,  $f \wedge g$ ,  $f \vee g$ .
  - ③ If  $f$  and  $g$  are *path formulas* then  $Xf$ ,  $Ff$ ,  $Gf$ ,  $fUg$ , and  $fRg$ .

# CTL\* Formal Semantics

- CTL\* semantics are defined in terms of a Kripke structure.
- Given a Kripke structure  $M = \langle S, S_0, R, L \rangle$ , a state  $s$  in  $M$  and a state formula  $f$ , the notation:

$$M, s \models f$$

means that  $f$  is true in  $M$  at state  $s$ .

- Given a path  $\pi$  through  $M$ , and a path formula  $g$ , the notation:

$$M, \pi \models g$$

means that  $g$  is true in  $M$  over path  $\pi$ .

- Also referred to as  $M, s$  models  $f$ , or  $M, s$  satisfies  $f$ .

## CTL\* Formal Semantics

Given a Kripke structure  $M = \langle S, S_0, R, L \rangle$ . Let  $p \in AP$  be an atomic proposition,  $f_1$  and  $f_2$  be *state formulas*,  $g_1$  and  $g_2$  be *path formulas*:

- 1  $M, s \models p$  iff  $p \in L(s)$
- 2  $M, s \models \neg f_1$  iff  $M, s \not\models f_1$
- 3  $M, s \models f_1 \vee f_2$  iff  $M, s \models f_1$  or  $M, s \models f_2$ .
- 4  $M, s \models f_1 \wedge f_2$  iff  $M, s \models f_1$  and  $M, s \models f_2$ .
- 5  $M, s \models \mathbf{E}g_1$  iff there is a path  $\pi$  starting at  $s$  such that  $M, \pi \models g_1$ .
- 6  $M, s \models \mathbf{A}g_1$  iff for every path  $\pi$  starting at  $s$ ,  $M, \pi \models g_1$ .

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- 1  $M, \pi \models f_1$  iff  $s$  is the first state in  $\pi$  and  $M, s \models f_1$ .
- 2  $M, \pi \models \neg g_1$  iff  $M, \pi \not\models g_1$
- 3  $M, \pi \models g_1 \vee g_2$  iff  $M, \pi \models g_1$  or  $M, \pi \models g_2$ .
- 4  $M, \pi \models g_1 \wedge g_2$  iff  $M, \pi \models g_1$  and  $M, \pi \models g_2$ .
- 5  $M, \pi \models \mathbf{X} g_1$  iff  $M, \pi^1 \models g_1$ .
- 6  $M, \pi \models \mathbf{F} g_1$  iff there exists a  $k \geq 0$  such that  $M, \pi^k \models g_1$ .
- 7  $M, \pi \models \mathbf{G} g_1$  iff for all  $k \geq 0$ ,  $M, \pi^k \models g_1$ .
- 8  $M, \pi \models g_1 \mathbf{U} g_2$  iff there exists a  $k \geq 0$  such that  $M, \pi^k \models g_2$  and for all  $0 \leq i < k$ ,  $M, \pi^i \models g_1$ .
- 9  $M, \pi \models g_1 \mathbf{R} g_2$  iff for all  $j \geq 0$ , if for every  $i < j$   $M, \pi^i \not\models g_1$  then  $M, \pi^j \models g_2$ .

## Examples:

- $M, s \models \mathbf{EF} p$
- $M, s \models \mathbf{AF} p$
- $M, s \models \mathbf{EG} p$
- $M, s \models \mathbf{AG} p$

- stands for "Linear-Time Logic"
- is a subset of CTL\*
- all formulas are (implicitly) universally quantified
- no explicit path quantifiers are used in state formulas (i.e. all state formulas are atomic)
- Provides operators for describing events along a *single* path.
- Example: **FG**  $p$   
At some point in the future, all the following states will have the property  $p$ .

- stands for "Computational-Tree Logic"
- subset CTL\* where only *state* formulas are allowed.
- every temporal operator (**F**, **G**, **X**, **U**, **R**) must be quantified.
- Example: **EFAAG**  $p$
- CTL operators:
  - 1 **AX** and **EX**
  - 2 **AF** and **EF**
  - 3 **AG** and **EG**
  - 4 **AU** and **EU**
  - 5 **AR** and **ER**

# The Model Checking Problem

- Using the previous definitions, the Model-Checking problem can be defined as follows:

$$M \models \phi$$

- Given:
  - 1 a finite model  $M$  represented as a Kripke structure, and
  - 2 a specification formula  $\phi$  specified in TL,check whether the model satisfies the given formula.



## Frequently-Used Properties

- Safety: "Something bad will *never* happen"

$$M \models \mathbf{G} \neg p$$

- Liveness: "Something good will *eventually* happen"

$$M \models \mathbf{F} p$$

# Finite State Machines

## Definition (Finite State Machine)

A Finite State Machine (FSM)  $\mathcal{A}$  is defined as a 5-tuple:

$$\mathcal{A} = \langle Q, \Sigma, \Delta, Q_0, F \rangle$$

where:

- $Q$  is a finite set of states,
- $\Sigma$  is a finite *alphabet*,
- $\Delta \subseteq Q \times \Sigma \times Q$  is a *transition relation*,
- $Q_0 \subseteq Q$  is a set of *initial states*,
- $F \subseteq Q$  is a set of *final states*.

# FSM Acceptance

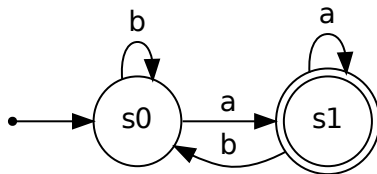
- A FSM accepts a word  $w \in \Sigma^*$  if there is a sequence of states  $s_0, s_1, \dots, s_n$  such that:
  - 1  $s_0 \in Q_0$ ,
  - 2  $s_n \in F$ ,
  - 3 for each  $1 \leq i \leq n$ ,  $(s_{i-1}, w_i, s_i) \in \Delta$ , where  $w_i$  is the  $i$ -th character of  $w$ .
- The language of a FSM  $\mathcal{A}$ , denoted  $\mathcal{L}(\mathcal{A})$ , is the set of all words accepted by  $\mathcal{A}$ .

# FSM Example

**Example:**

$$\mathcal{A}_1 = \langle \{s_0, s_1\}, \{a, b\}, \Delta, \{s_0\}, \{s_1\} \rangle$$

where:  $\Delta = \{(s_0, b, s_0), (s_0, a, s_1), (s_1, a, s_1), (s_1, b, s_0)\}$



This FSM accepts all words that end with an a.

# Büchi Automata

- A Büchi Automaton is a FSM that recognizes *infinite* words.
- This concept is called  $\omega$ -acceptance.

## Definition (Büchi Automaton)

A Büchi Automaton  $\mathcal{B}$  is defined as a 5-tuple:

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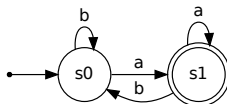
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# Büchi Automaton Acceptance ( $\omega$ -acceptance)

- A Büchi Automaton has a finite number of states.
- However, it recognizes infinite words.
- Therefore, some of the states have to be visited *infinitely many* times.
- A Büchi Automaton accepts a word  $w$  if there is an infinite path  $\rho = s_0, s_1, \dots$  such that:
  - 1  $s_0 \in Q_0$ ,
  - 2 For all  $i \geq 1$ ,  $(s_{i-1}, w_i, s_i)$ ,
  - 3 If  $\text{inf}(\rho)$  denotes the set of states visited *infinitely-many* times in  $\rho$ , then  $\text{inf}(\rho) \cap F \neq \emptyset$ .
- A Büchi Automaton accepts a word if at least one of the final states is visited infinitely-many times.
- The language of a Büchi Automaton  $\mathcal{B}$ , denoted  $\mathcal{L}(\mathcal{B})$  is the set of all (infinite) words it accepts.
- Note that  $\mathcal{L}(\mathcal{B}) \subseteq \Sigma^\omega$ , where  $\Sigma^\omega$  is the set of infinite words over  $\Sigma$ .

# Büchi Automaton Example

The following Büchi Automaton accepts all words that have infinitely-many a's:



- For example, it accepts the word  $(ab)^\omega = ababab\dots$
- In general, it accepts words described by the follows  $\omega$ -regular expression  $(b^*a)^\omega$ .

# From Kripke to Büchi

Convert a Kripke structure  $M = \langle S, S_0, R, L \rangle$  over atomic propositions  $AP$  to a Büchi automaton  $\mathcal{B} = \langle Q, \Sigma, \Delta, Q_0, F \rangle$  such that:

- 1  $Q = S \cup \{i\}$ ,
- 2  $\Sigma = \mathcal{P}(AP)$ , (i.e. each transition is labeled with a subset of  $AP$ )
- 3 Same transitions as the Kripke structure in addition to:
  - 1 Transitions going from  $i$  to each of the start states in  $S_0$ .
  - 2 Each transition is *labeled* with the set of predicates of the *target state*.
- 4  $Q_0 = \{i\}$
- 5  $F = Q$ , (All states are accept states)

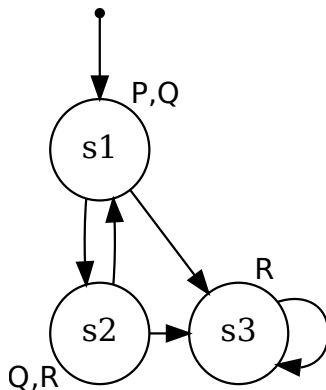
The resulting Büchi Automaton accepts words equivalent to possible state sequences in the Kripke structure.



## From Kripke to Büchi (Example)

### Example:

Convert the following Kripke structure, defined over  $AP = \{P, Q, R\}$ , to a Büchi automaton:



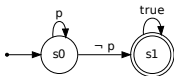
# Modeling LTL Properties with Büchi Automata

- Every LTL formula over  $AP$  can be modeled as a Büchi automaton with alphabet  $\Sigma = \mathcal{P}(AP)$ .
- The language of the Büchi automaton is the set of *paths* that *satisfy* the LTL formula.
- Examples:

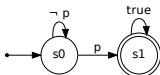
- **G**  $p$



- $\neg$ **G**  $p$



- **F**  $p$



# LTL Model Checking with Büchi Automata

Given a model  $M$  represented as a Kripke structure, and an LTL formula  $\phi$ , the following algorithm decides whether  $M \models \phi$ :

- 1 Convert  $M$  to a Büchi Automaton  $\mathcal{B}_1$ .
- 2 Construct a Büchi Automaton  $\mathcal{B}_2$  equivalent to the *negation* of  $\phi$  ( $\neg\phi$ ).
- 3 Construct a Büchi Automaton  $\mathcal{B}_3$  that recognizes the language  $\mathcal{L}(\mathcal{B}_3) = \mathcal{L}(\mathcal{B}_1) \cap \mathcal{L}(\mathcal{B}_2)$ , by calculating the *cross-product* for  $\mathcal{B}_1 \times \mathcal{B}_2$ .
- 4 Check the language of  $\mathcal{B}_3$  for emptiness:
  - If the language is empty, then  $\phi$  *holds* in  $M$ .
  - If not, then  $\phi$  *does not hold* in  $M$ . Any word  $w \in \mathcal{L}(\mathcal{B}_3)$  is a counter-example.

# Emptiness Check for Büchi Automata

Given a Büchi Automaton  $\mathcal{B}_3$ , the following algorithm determines whether its language is empty.

- 1 Determine the *strongly-connected components* (SCC) in  $\mathcal{B}_3$ .
- 2 If there is a *reachable, non-trivial* strongly-connected component that *contains a final state*, then the language is *not* empty. Otherwise, the language is empty.

Notes:

- A *trivial* SCC, is one that contains only 1 state without a self-transition.
- A *reachable* SCC, is one that can be reached from a start state.

# Time Complexity of Model Checking

- There exist several model checking algorithms.
- The best ones currently have the following upper-bound time-complexities for a formula  $\phi$  and model  $M$ :
  - LTL:  $O(|M| \cdot 2^{|\phi|})$
  - CTL:  $O(|M| \cdot |\phi|)$
  - CTL\*:  $O(|M| \cdot 2^{|\phi|})$

$|M| = n + m$ , where  $n$  is the no. of states, and  $m$  is the no. of transitions.

- The following lower-bounds have also been proven for model-checking:
  - LTL: PSPACE-Complete
  - CTL: P-Complete
  - CTL\*: PSPACE-Complete

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- The following are the major results:
  - Ordered binary decision diagrams (OBDDs):  
Works on synchronous systems and has been used for systems with up-to  $10^{120}$  states.

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- One of the major-challenges facing model checking.
- Refers to the exponential increase in the number of possible states with processes and data.
- A system with  $n$  asynchronous processes, each having  $m$  states has up-to  $m^n$  states.
- State transition system for  $n$ -bits of data has  $2^n$  states.
- A lot of research has been (and is being) done on the state-explosion problem.
- The following are the major results:
  - Ordered binary decision diagrams (OBDDs):  
Works on synchronous systems and has been used for systems with up-to  $10^{120}$  states.
  - Partial order reduction: Works on asynchronous systems and exploits certain *mutual-independence* properties of parallel processes.

# SPIN and Promela

- LTL model checker.
- SPIN stands for "**S**imple **P**romela **I**nterpreter"
- Model is specified in **Promela**
- Promela stands for "**P**rocess **M**eta **L**anguage"
- Supports parallel synchronous or asynchronous processes that communicate using global variables or message passing.

# Structure of a Promela Model Specification

- A Promela specification consists of:
  - type declarations
  - channel declarations
  - variable declarations
  - process declarations
  - Optionally: `init` process
- since the model needs to be finite, data, channels and processes must be bounded.

# Process Declaration in Promela

- A process is declared using the `proctype` keyword.
- Process declaration consists of:
  - 1 process name
  - 2 list of parameters
  - 3 local variable declaration
  - 4 body



# Promela Statements

- Promela statements can be either *executable* or *blocked*
- A blocked statement blocks the execution until the statement becomes *unblocked*
- statements:
  - skip: always executable
  - assert(<expr>): asserts that <expr> should always be true. always executable.
  - expression: executable if not zero.
  - assignment: always executable.
  - if :: fi: Provides non-deterministic choice. Executable if at least one choice is executable.
  - do :: od: Like if but repeats. Executable if at least one choice is executable.
  - break: Exits a do statement. Always executable.

# Mutual Exclusion Problem

- Organizing access to a shared resource such that:
  - ① At most 1 process uses the resource at any given time.
  - ② Every interested process can eventually get access to the resource.
- The program part that accesses a shared resource is called the *critical region*.

# Phony Mutual Exclusion Algorithm




```
int flag = 0;

void enter_critical() {
    while(flag != 0);
    flag = 1;
    critical_region();
    flag = 0;
}
```

- Flaw: If process 2 reads the flag before process 1 sets it to 1, both processes will enter critical region at the same time.

# Using SPIN to Discover the Bug

# References

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*Thank you*